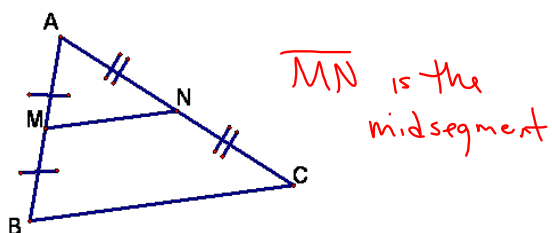
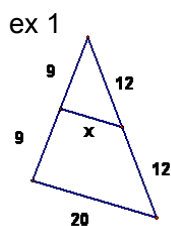
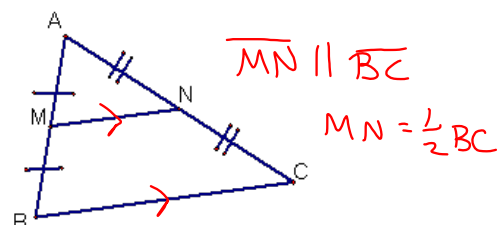


## 5.1 Midsegment Theorem and Coordinate Proof

**Midsegment** of a triangle is a segment whose endpoints are the midpoints of two sides of a triangle.

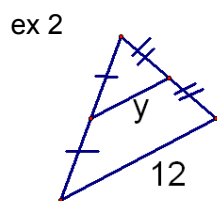


**Theorem 5.1- Midsegment theorem** A midsegment of a triangle is parallel to one side of the triangle, and its length is  $\frac{1}{2}$  the length of that side.



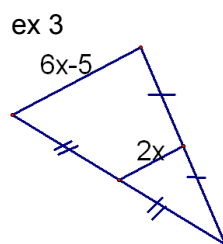
$$x = \frac{1}{2} 20$$

$$x = 10$$



$$y = \frac{1}{2} 12$$

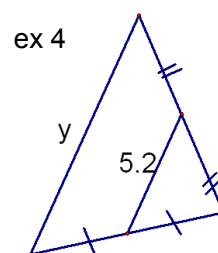
$$y = 6$$



$$2x = \frac{1}{2} (6x - 5)$$

$$4x = 6x - 5$$

$$x = 2.5$$



$$5.2 = \frac{1}{2} y$$

$$10.4 = y$$

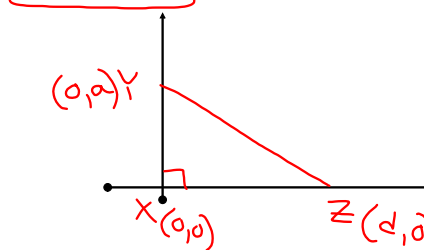
## Coordinate Proof

Tips

1. Use Origin as vertex or center
2. At least one side on x-axis
3. 1st Quadrant if possible
4. Use easiest coordinates possible

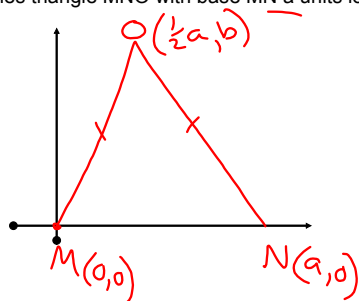
## Example 5

Right triangle XYZ with hypotenuse  $\overline{YZ}$   
 $XZ = d$  units long



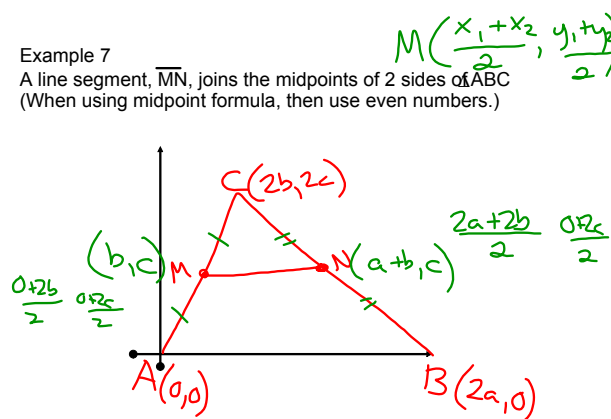
## Example 6

Isosceles triangle MNO with base  $\overline{MN}$  a units long

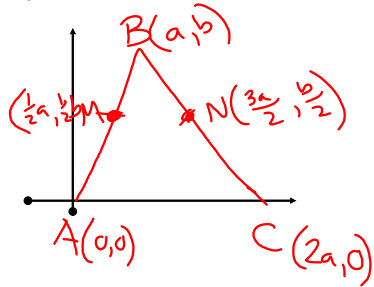


## Example 7

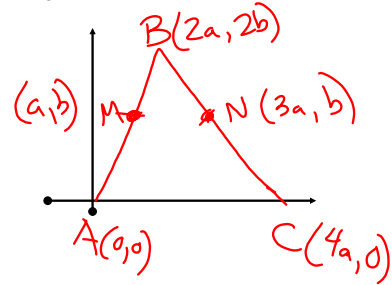
A line segment,  $\overline{MN}$ , joins the midpoints of 2 sides of  $\triangle ABC$   
 (When using midpoint formula, then use even numbers.)



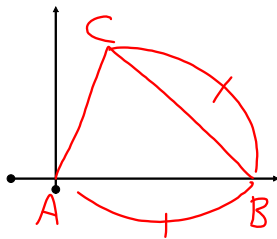
## Example 8

Isosceles triangle ABC (legs  $\overline{AB}$  with midpoint M, and  $\overline{CB}$  with midpoint N)

## Example 8

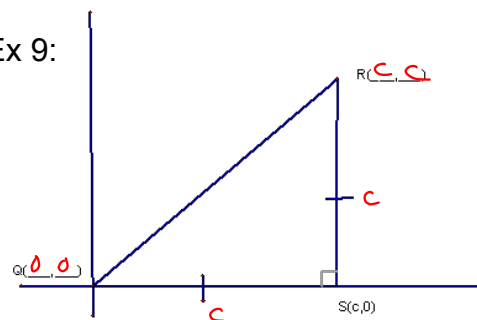
Isosceles triangle ABC (legs  $\overline{AB}$  with midpoint M, and  $\overline{CB}$  with midpoint N)

## Example 8

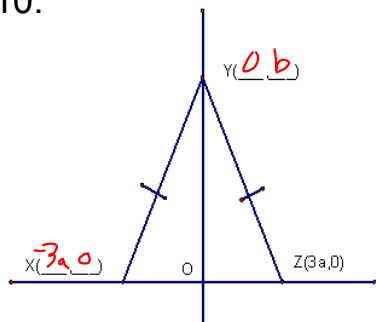
Isosceles triangle ABC (legs  $\overline{AB}$  with midpoint M, and  $\overline{CB}$  with midpoint N)

Fill in the missing coordinates.

Ex 9:



Ex 10:



Coordinate Proof

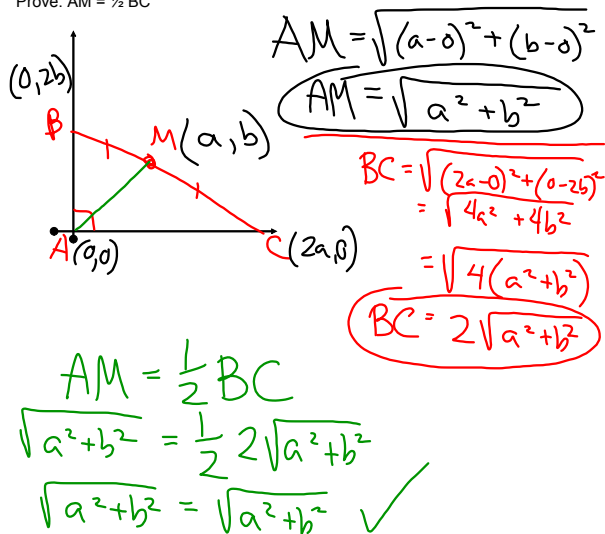
Distance Formula  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ Slope  $m = \frac{y_2 - y_1}{x_2 - x_1}$  Show  $\parallel$  (parallel)  $\perp$  (perpendicular)

Midpoint Formula

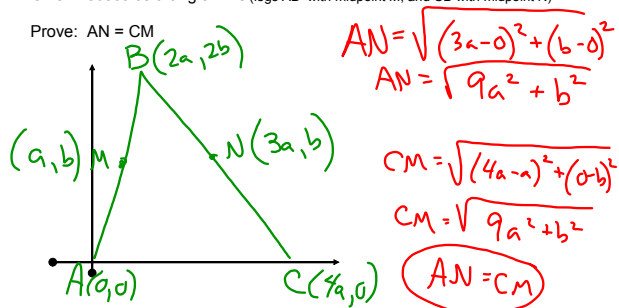
$$\left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

When using midpoint formula, then use even numbers.

Example

Prove that the measure of the segment that joins the vertex of a right  $\triangle$  to midpoint of the hypotenuse =  $\frac{1}{2}$  the measure of the hypotenuseGiven: Right  $\triangle ABC$  with hypotenuse  $\overline{BC}$ . (M is the midpoint of  $\overline{BC}$ .)Prove:  $AM = \frac{1}{2} BC$ 

The segments joining the vertices to the midpoints of the legs of an isosceles triangle are congruent.

Given: Isosceles triangle ABC (legs  $\overline{AB}$  with midpoint M, and  $\overline{CB}$  with midpoint N)Prove:  $AN = CM$ 

HW

Use example 7 from notes to prove the  
midsegment theorem and  
p298-299 #s 3-5, 15-19, 24